

# Machine Learning Based State Estimation for PMU-Unobservable Transmission Systems – TVA Case Study



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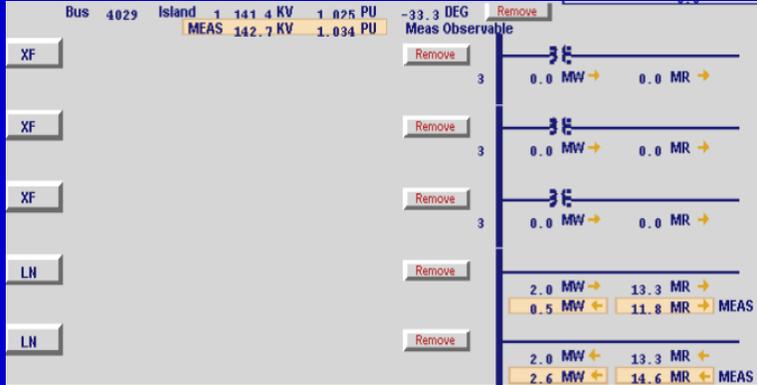
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**NASPI Work Group Meeting**  
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**Salt Lake City, UT**

# State Estimation

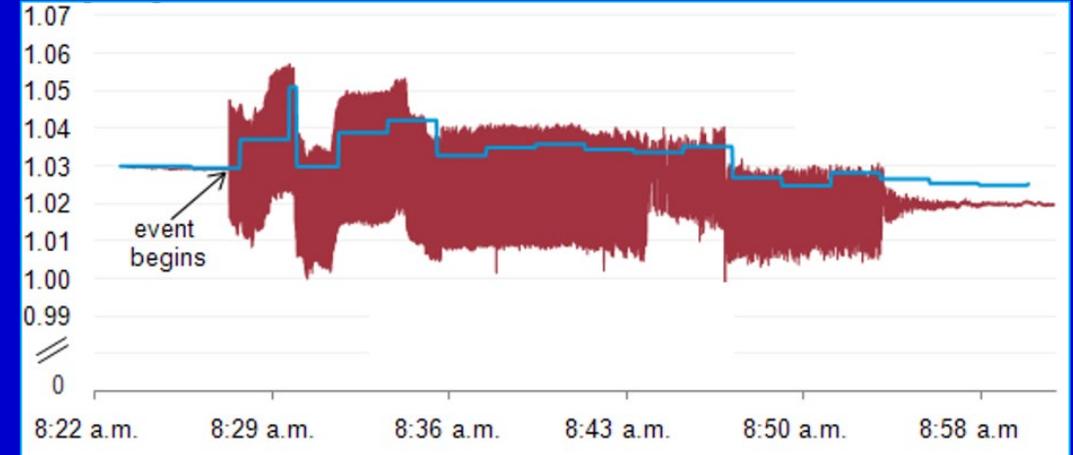
## *Backbone EMS Function for Situational Awareness*

### SCADA/EMS State Estimation



- **State Definition [x]:** Positive sequence voltage phasors (bus voltage magnitudes and angles) of system's buses
- **Measurement Set [z]:** SCADA data
  - Voltage magnitude, current magnitude, real & reactive power flows and injections
  - Measurement model: Nonlinear
  - Gaussian distribution of measurement error
- **Solution Algorithm:** Weighted Least Squares
  - Iterative Solution

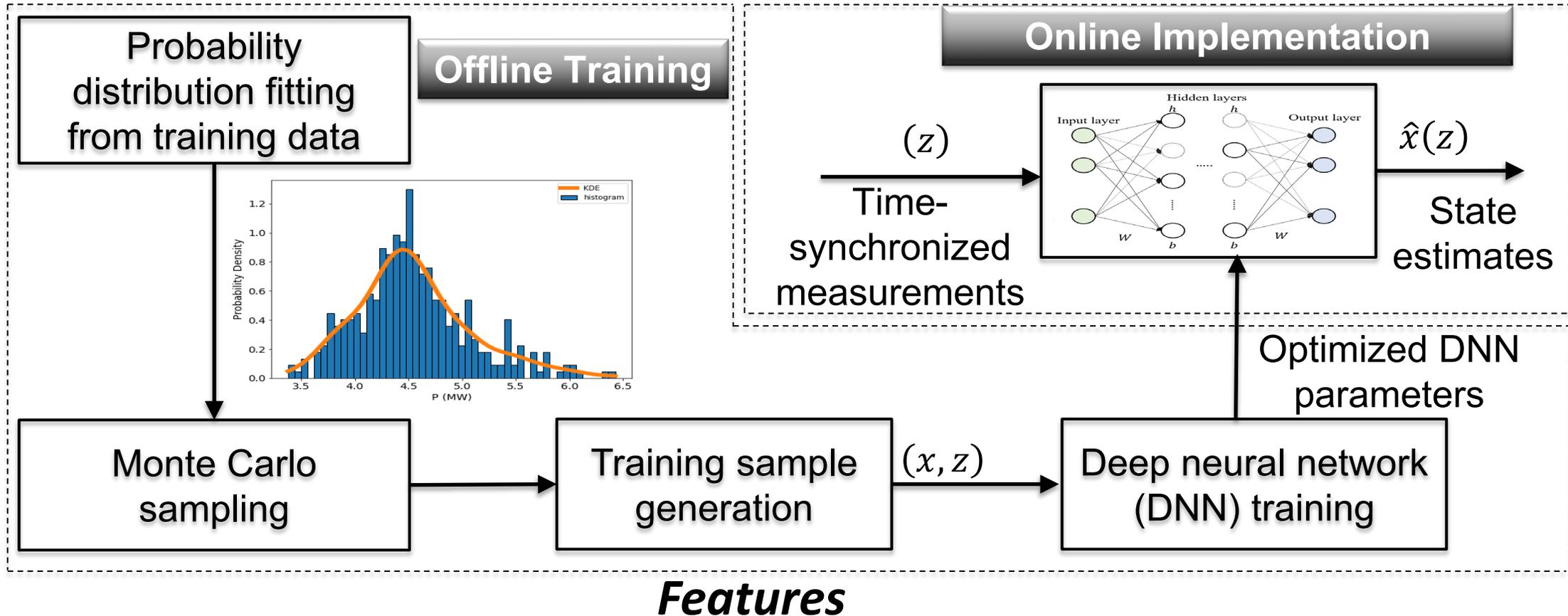
### PMU Based State Estimation



- a.k.a Linear State Estimation
- **Measurement Set [z]:** Phasor Measurement Unit (PMU)
  - Voltage and current phasors
  - Measurement model: Linear
  - Gaussian distribution of measurement error
- **Solution Algorithm:** Weighted Least Squares
  - Direct Solution

# Objective

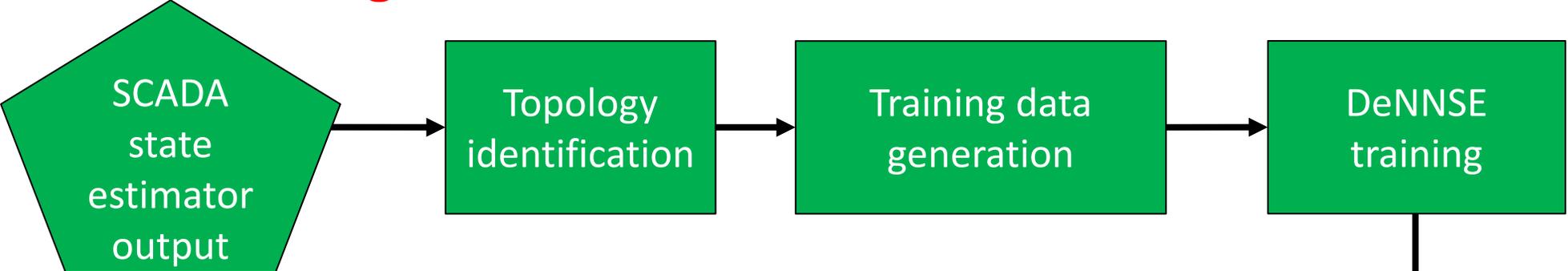
## Development of a Machine-Learning Based State Estimator



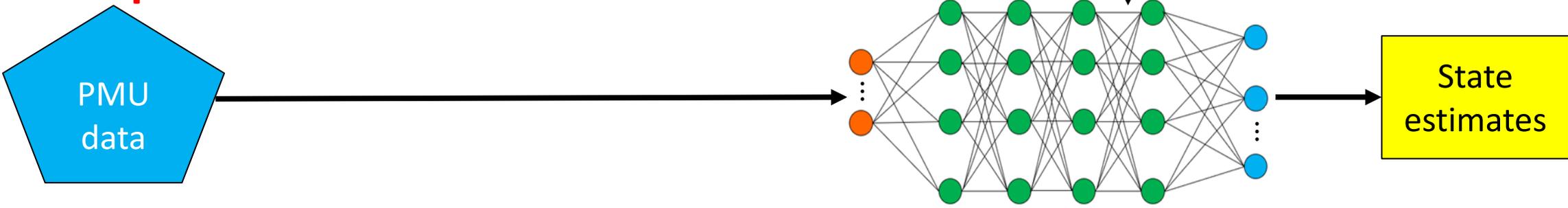
- Model Independent
- Independent of Measurement Error Distribution
- Overcomes SCADA/PMU Synchronization Issues
- Achieves Full System Observability with Limited Number of PMUs
- High Speed

# Deep Neural Network-based State Estimator (DeNNSE)

## Offline learning

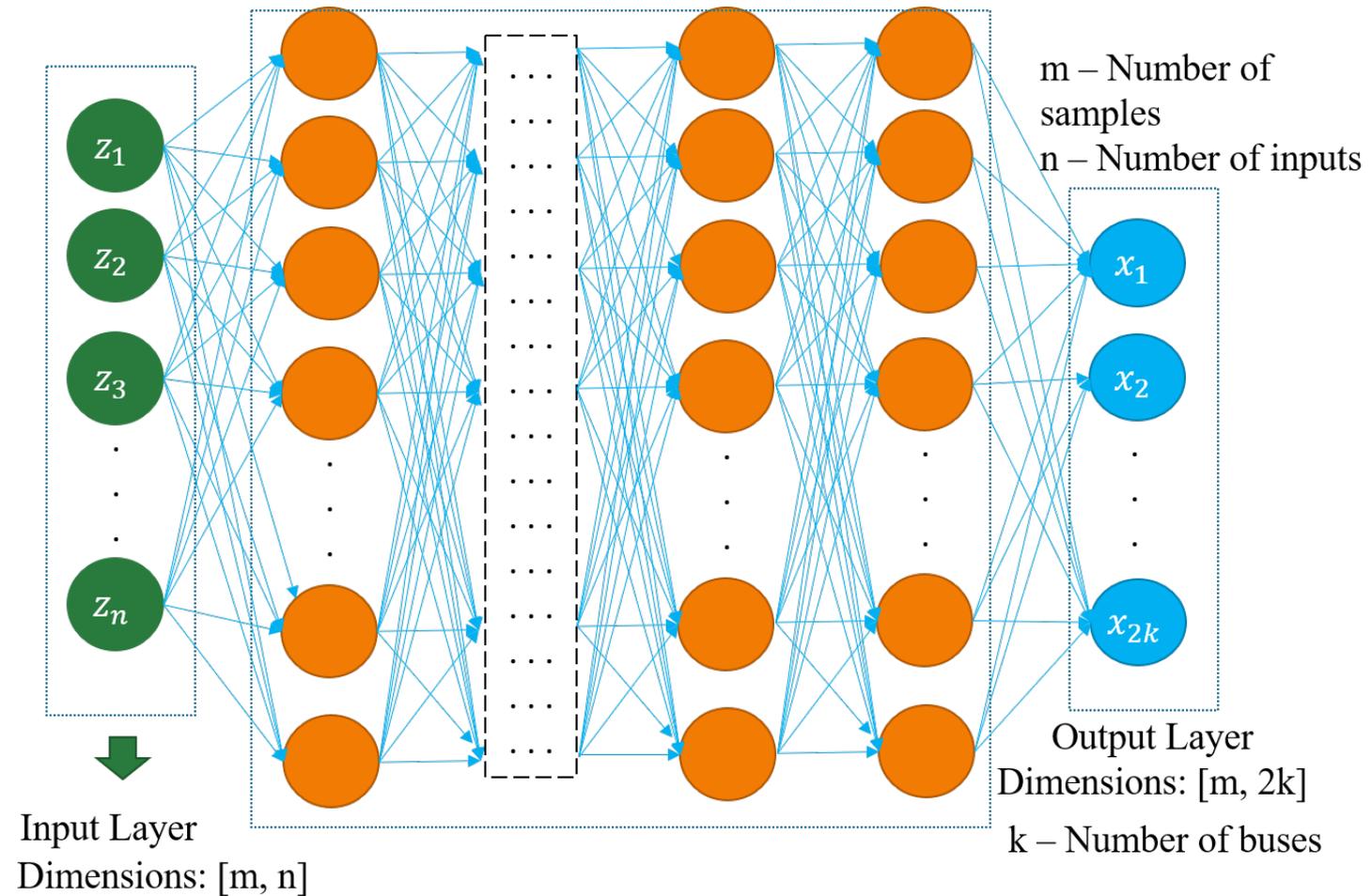


## Online implementation



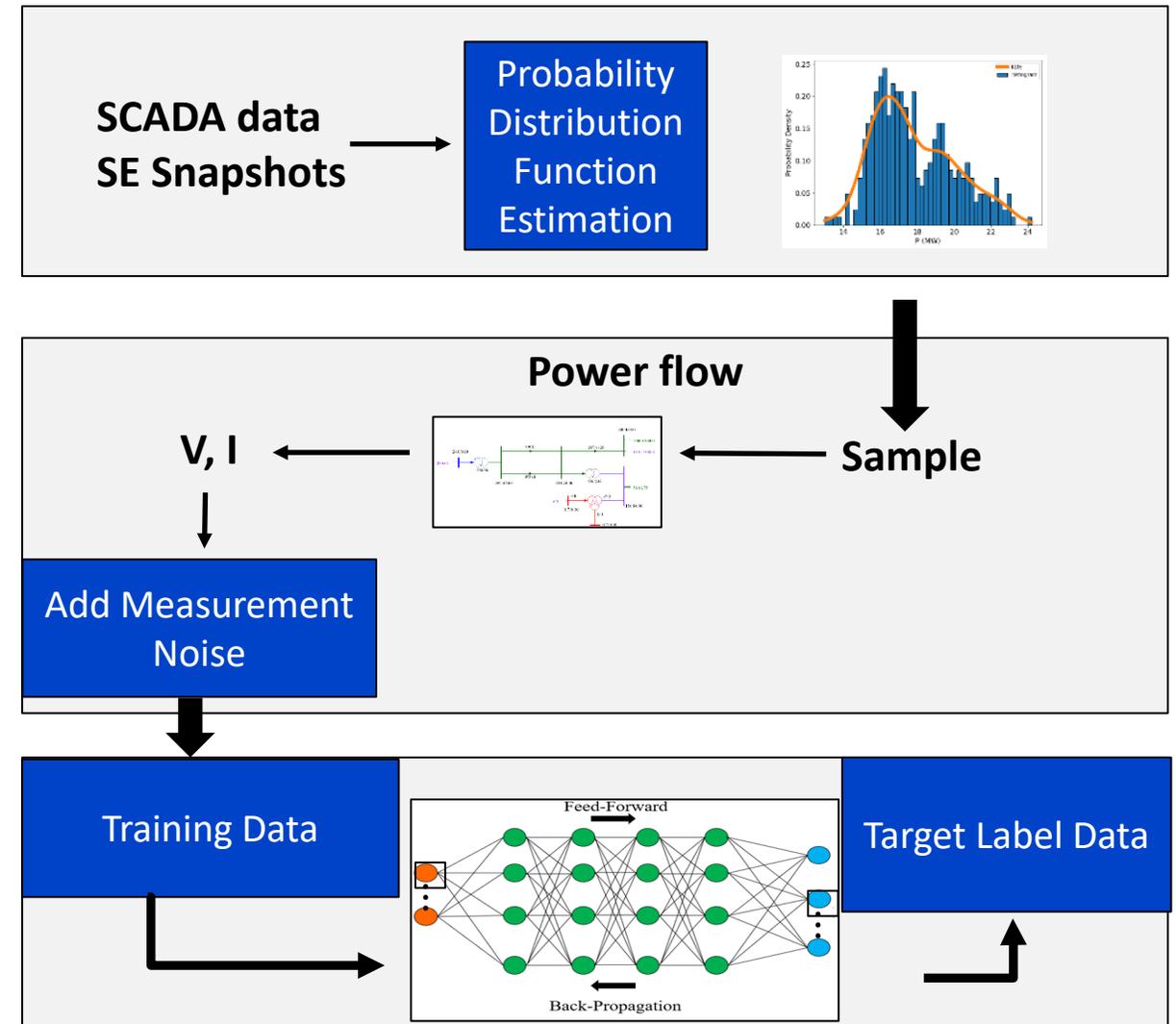
# Deep Neural Network (DNN)

- DNN Input: PMU measurements
- DNN Output: States of the system
- Target accuracy:
  - $<0.1\%$  error in magnitude
  - $<0.5^\circ$  error in angle



# DNN Training

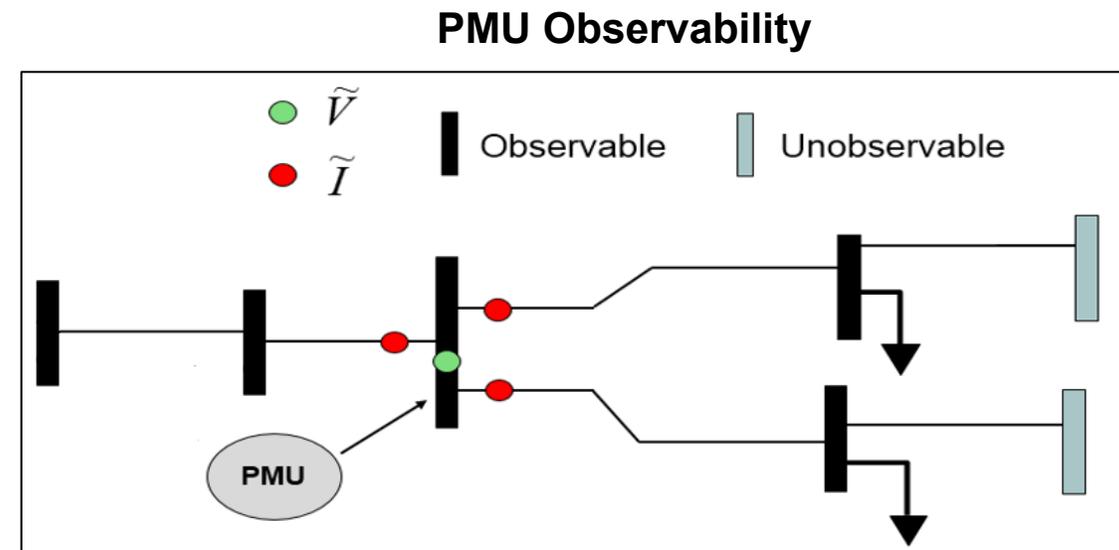
- Collect historical SE data (Load, generation, system model)
- Probability distribution function fitting
- Monte Carlo sampling and PF/OPF solution
- Embed noise functions to mimic instrumentation errors: “Synthetic Measurements”
- Identify dominant topologies
- Train DNN hyperparameters for base topologies and specific PMU placement



# LSE vs ML-SE - Topological Observability

## Full Grid Observability with Limited Number of PMUs

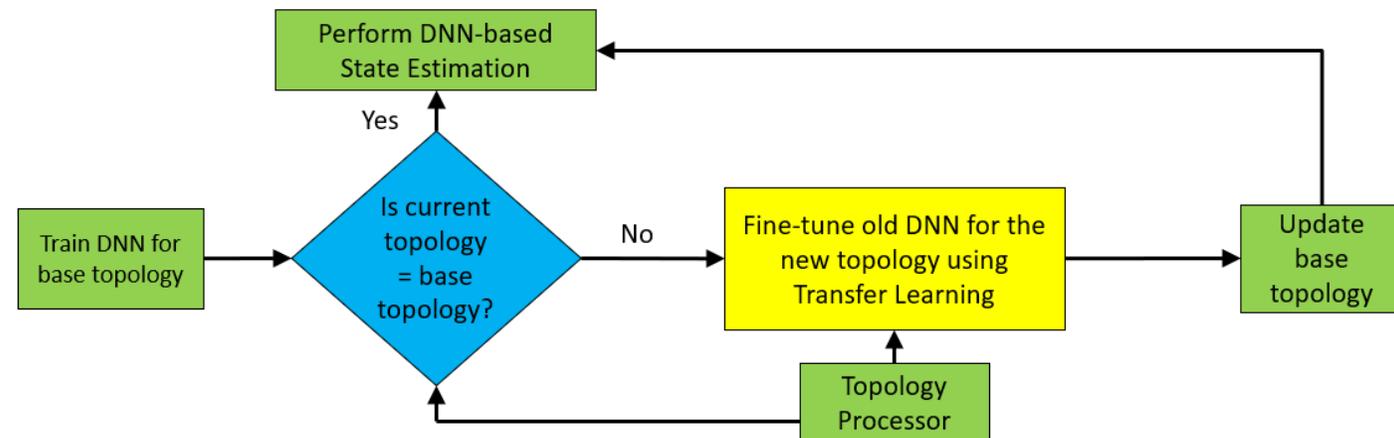
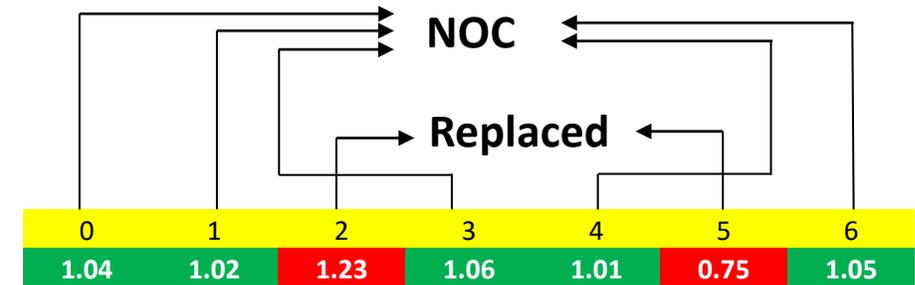
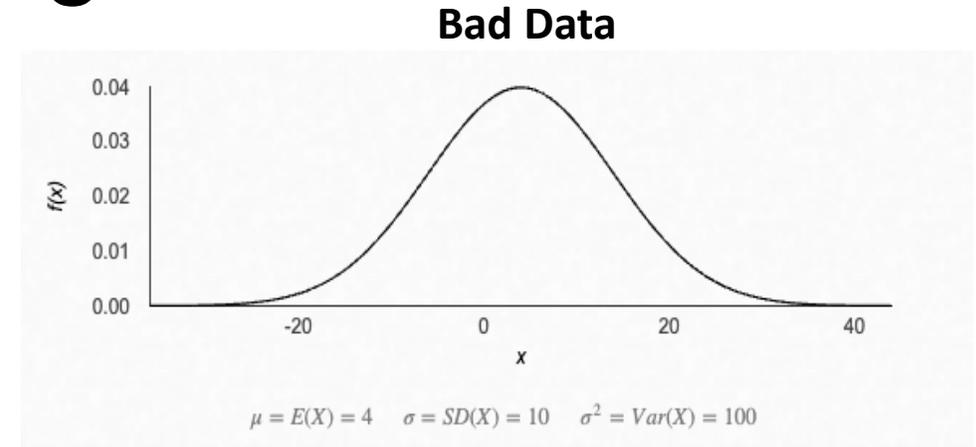
- Linear State Estimation (LSE): number of estimated states depends on topological observability from PMUs
- ML based SE: entire system state estimation without need for topological observability

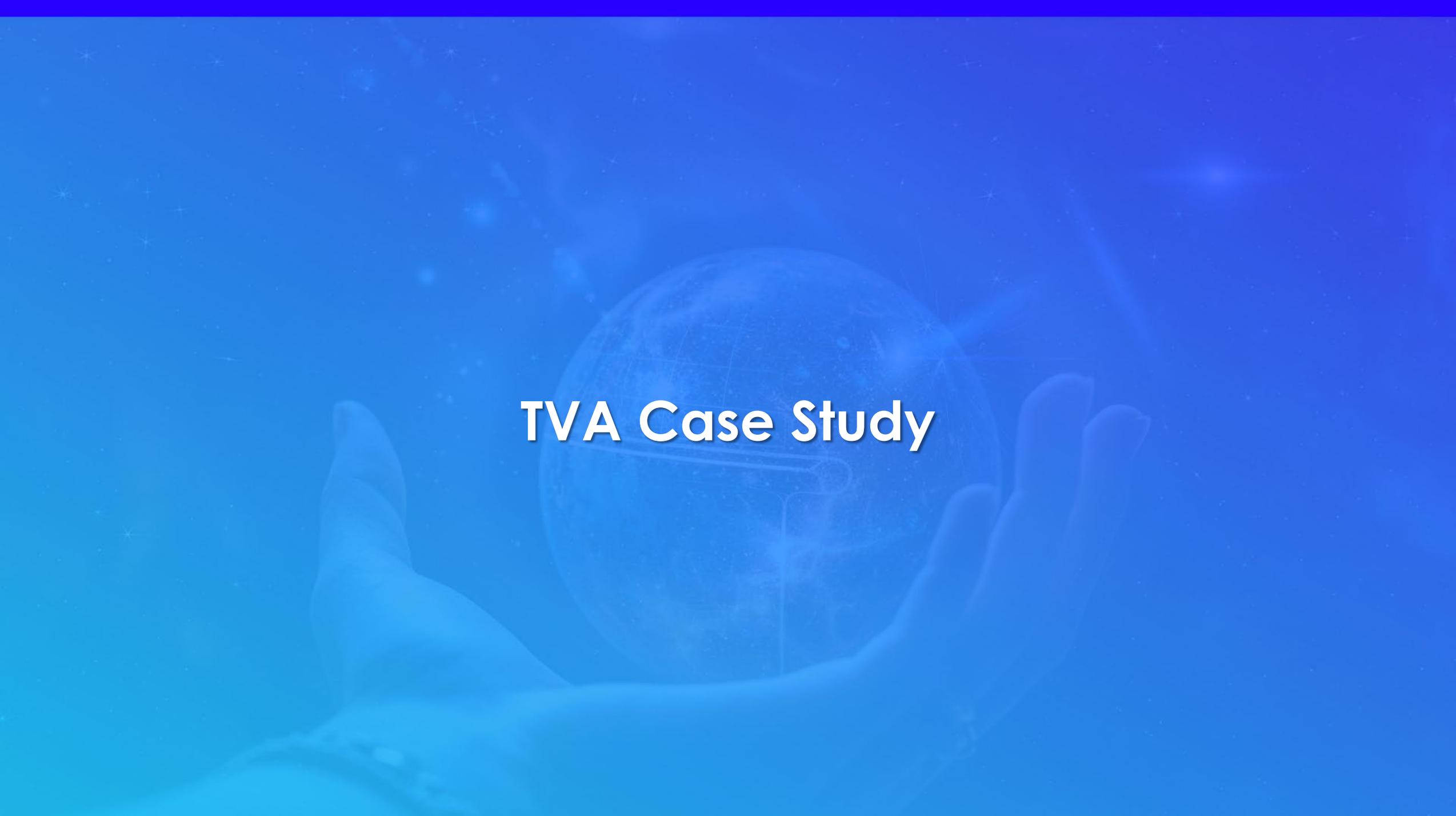


IEEE 118 Bus System – Estimation Error		
Scenario	LSE	ML-SE
<b>Metric</b>	<b>32 PMUs</b>	<b>13 PMUs</b>
Voltage Magnitude	0.00100 p.u.	0.0010 p.u.
Voltage Angle	0.00199 rad	0.0020 rad

# Bad/Missing Data & Topology Changes

- Bad/Missing data detection based on Wald Test
- Bad/Missing data replacement with Nearest Operating Condition (NOC) from training dataset
- Transfer Learning used for DNN update when topology changes





# TVA Case Study

# Data Received from TVA

## State Estimator Cases

- PSS/E .raw files from July 1 to December 31 (6 months)
- 2 files for each day (at 2:00 PM and 2:30 PM) → 366 files
- The TVA area was chosen for this study

## PMU Measurements

- PMU data for 5 days of 5 months (2:00 PM – 3:00 PM in every file)



- PMU measurement data



- PMU data resolution: 1 sample/second
- 709 voltage and current measurement channels each

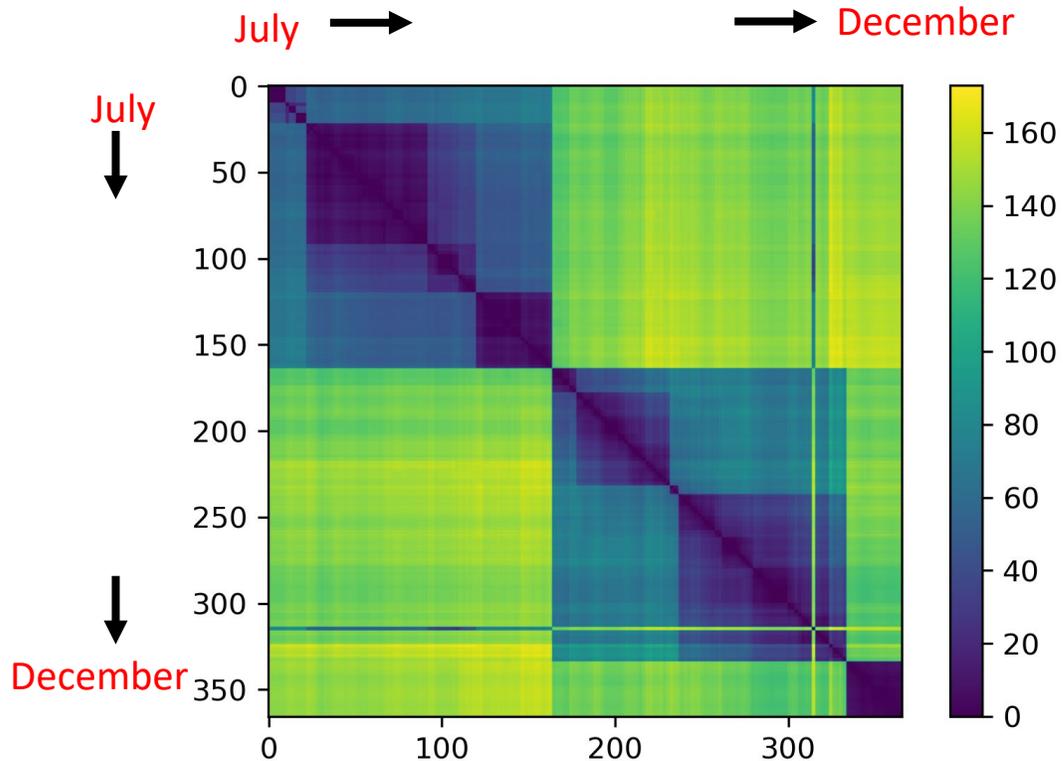
kV Level	#PMUs	#Substations
500	130	29
345	3	1
230	15	5
161	517	92
<=138	44	19

**PMU Observability: 20-25%**

# Topology Identification

- Topology clustering
  - Branch difference matrix for consecutive cases
  - Applied K-means clustering to the matrix

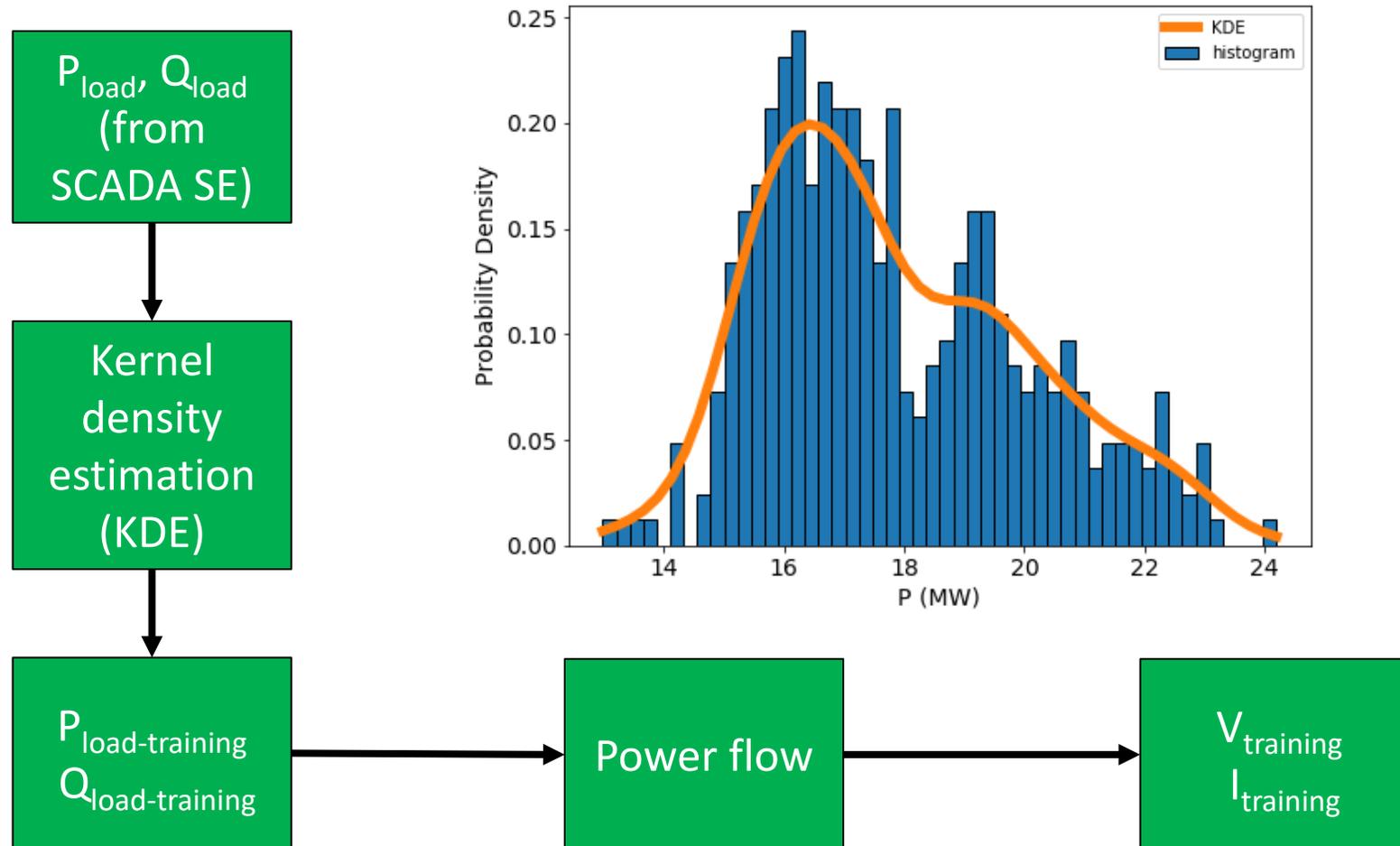
Branch Difference Matrix Heatmap



Cluster	Cases in each Cluster	Days in each Cluster
$T_1$	Case 1 to Case 22	July 1 to July 11
$T_2$	Case 23 to Case 92	July 12 to August 15
$T_3$	Case 93 to Case 120, Case 314, Case 315	August 16 to August 30, Dec. 10
$T_4$	Case 121 to Case 164	August 29 to Sep. 21
$T_5$	Case 165 to Case 178	Sep. 22 to Sep 28
$T_6$	Case 179 to Case 236	Sep 29 to Oct 27
$T_7$	Case 238 to Case 278	Oct 28 to Nov 17
$T_8$	Case 279 to Case 334 (excluding 314, 315)	Nov 18 to Dec 20, excluding Dec. 10
$T_9$	Case 335 to Case 366	Dec 21 to Dec 31

# DeNNSE Training Input

- DNN requires a large amount of data (big data) to learn the mapping relations between the input features and the output variables

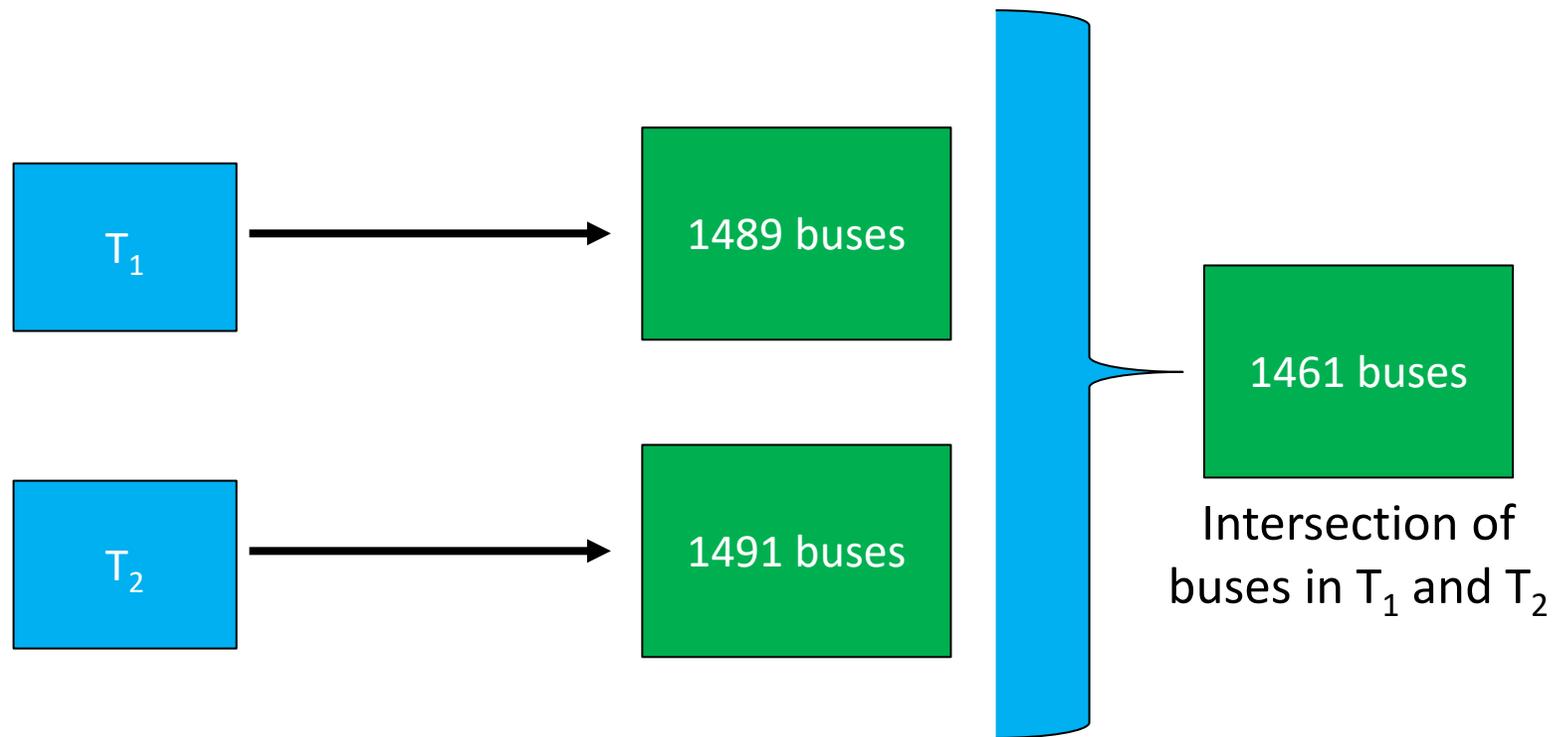


## Input Features

- 687 Voltage phasors
- 447 Current phasors
- From the obtained probability density functions (PDFs), 8,000 samples were generated for each feature

# DeNNSE Training Output

- DNN output: estimated states are voltages at 69 kV and higher, within the TVA area



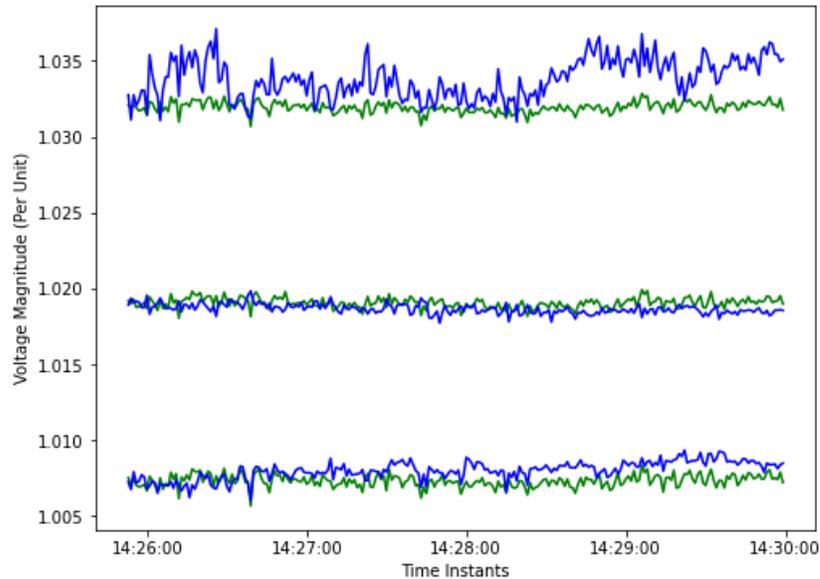
Voltage level (kV)	#States/Buses
500	52
345	1
230	17
161	1168
138	6
115	45
69	172

- The output dimension is determined considering the buses that are common to  $T_1$  and  $T_2$

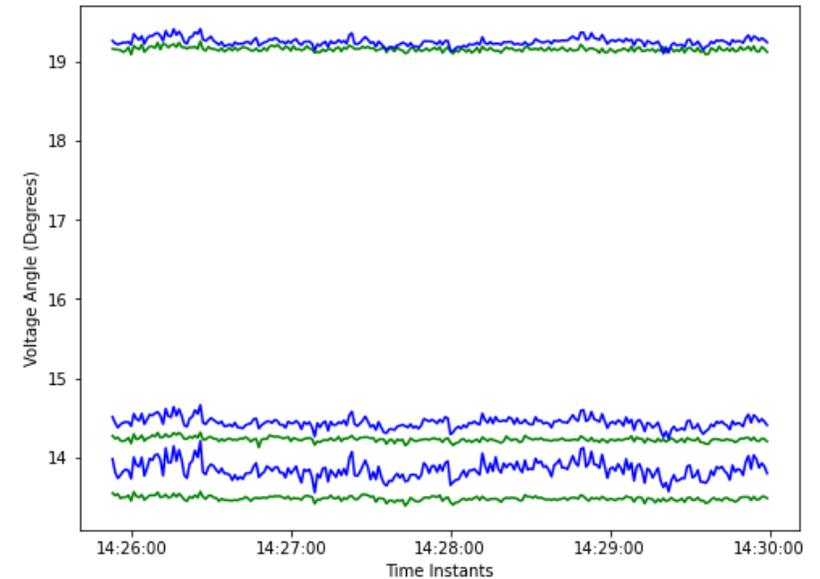
# DeNNSE Results - Training for $T_2$

- DNN is trained and tested on  $T_2$
- PMU data from Aug 15: 2:25 PM-2:30 PM is used for testing

Voltage magnitude (Per unit)



Voltage angle (Degrees)



— PMU Measurements

— Estimated States

# DeNNSE Results Summary with and without Transfer Learning

- To analyze the effectiveness of the transfer learning, two cases are studied
  - DeNNSE is trained and tested for  $T_2$
  - DeNNSE is trained on  $T_1$ , adapted to  $T_2$  using transfer learning, and then tested on  $T_2$
- The PMU data from Aug 15: 2:25 PM-2:30 PM is used for testing in both cases

DeNNSE trained for  $T_2$

Voltage Magnitude Error (%)	Voltage Angle Error (Degrees)
0.212	1.26

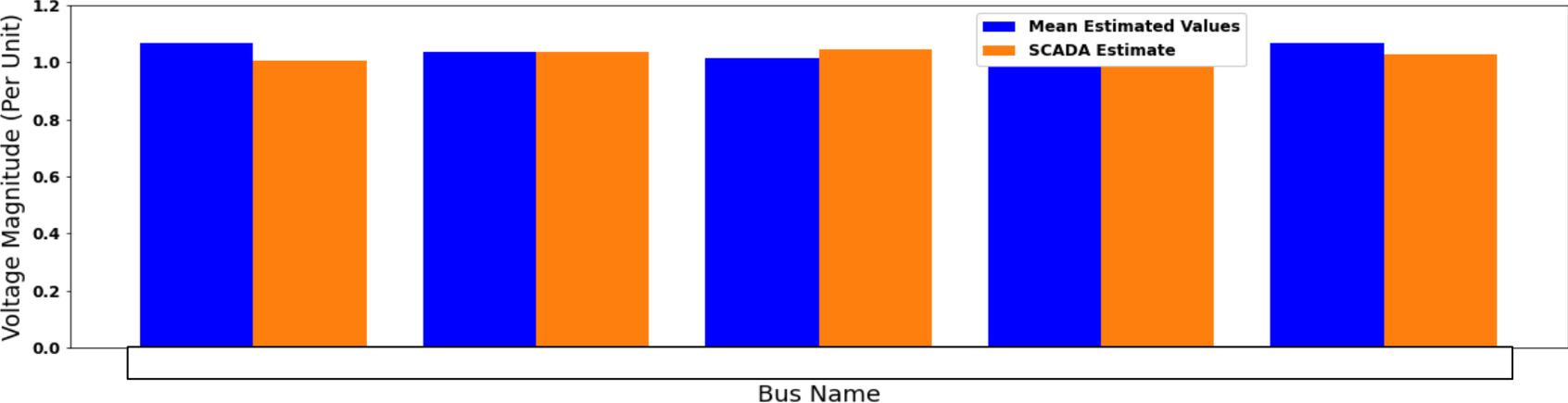
DeNNSE trained using  $T_1$  and updated using Transfer Learning for  $T_2$

Voltage Magnitude Error (%)	Voltage Angle Error (Degrees)
0.228	1.29

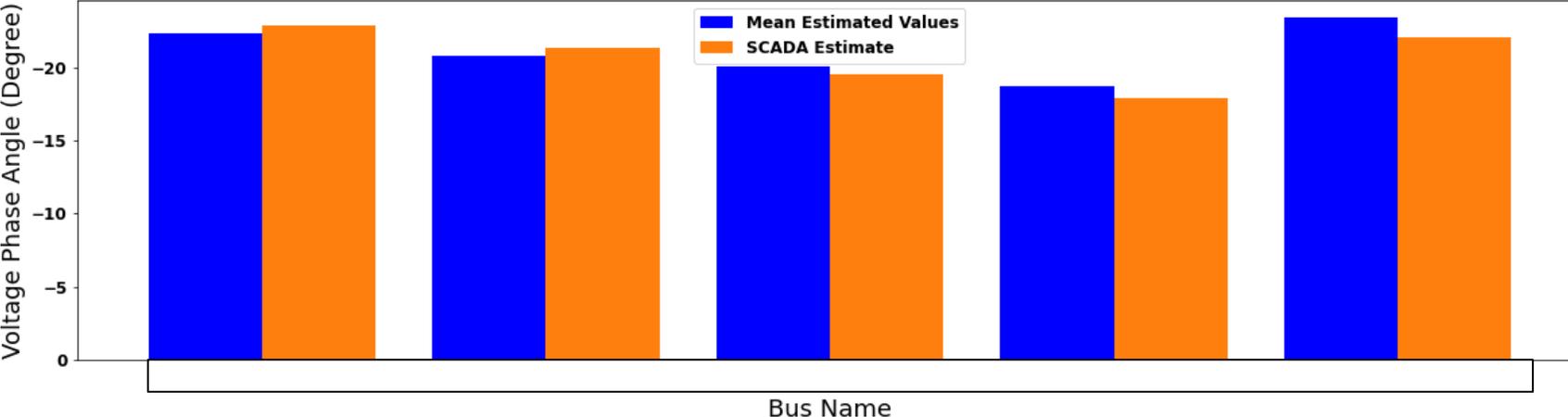
# DeNNSE Results - Comparison with SCADA State Estimator - 500kV

- Comparison between SCADA-SE and DeNNSE for August 15<sup>th</sup>
- SCADA-based state estimator output at 2:30 PM is compared with the mean value of DeNNSE obtained using PMU data between 2:25 PM-2:30 PM

Voltage Magnitude



Voltage Phase Angle



# Summary

## DeNNSE: ML & PMU-based state estimation

- 1) Achieves full system observability with limited number of PMUs
- 2) High speed
- 3) Avoids synchronization challenges between PMU and SCADA data
- 4) Model used only for training

DeNNSE applied to the TVA system

Satisfactory DeNNSE results despite the limited PMU coverage

# Project Participants





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