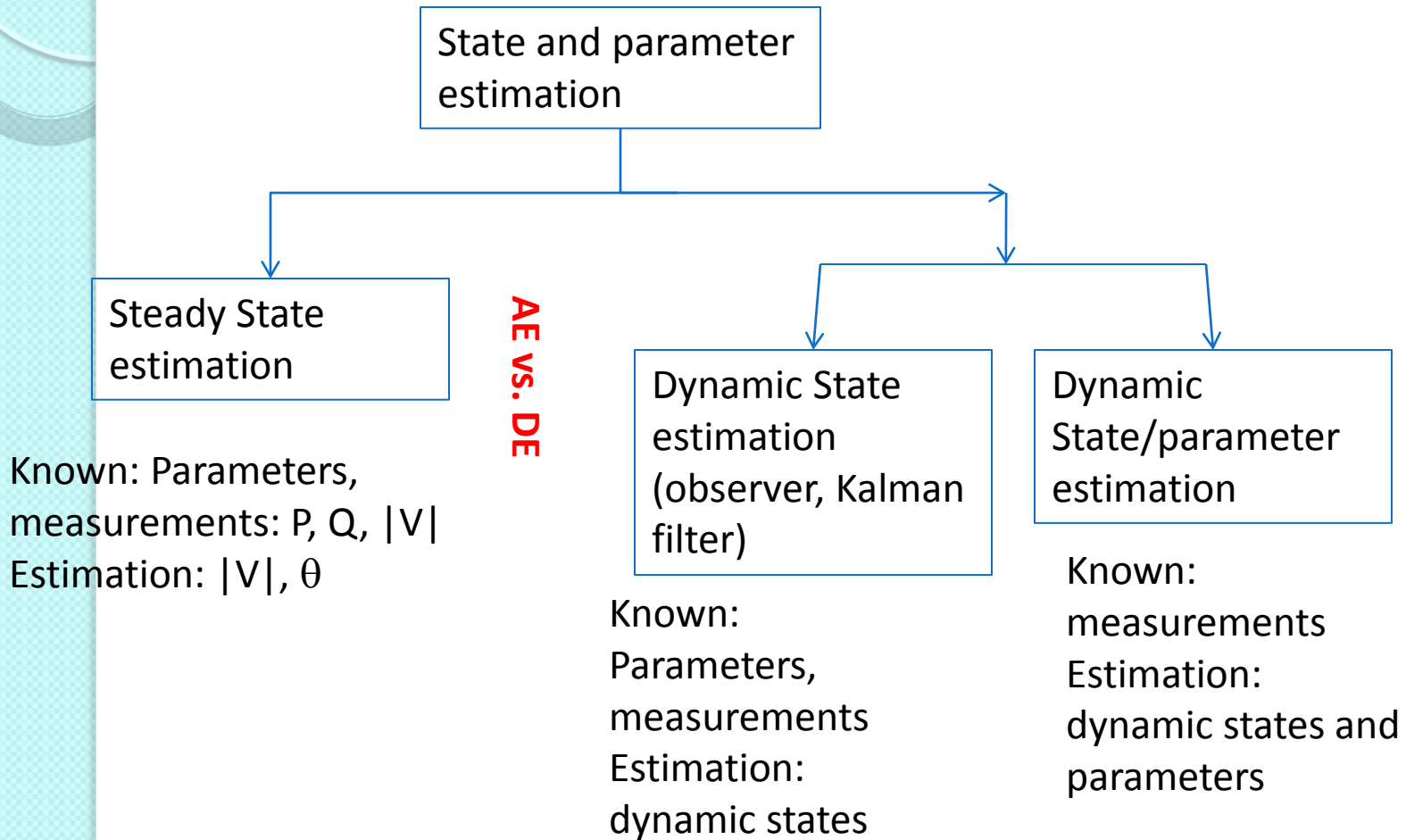


# Electromechanical Dynamic State and Parameter Estimation Using PMU Data

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# State and parameter estimation



# Machine parameter and state estimation using digital fault recorder (DFT)

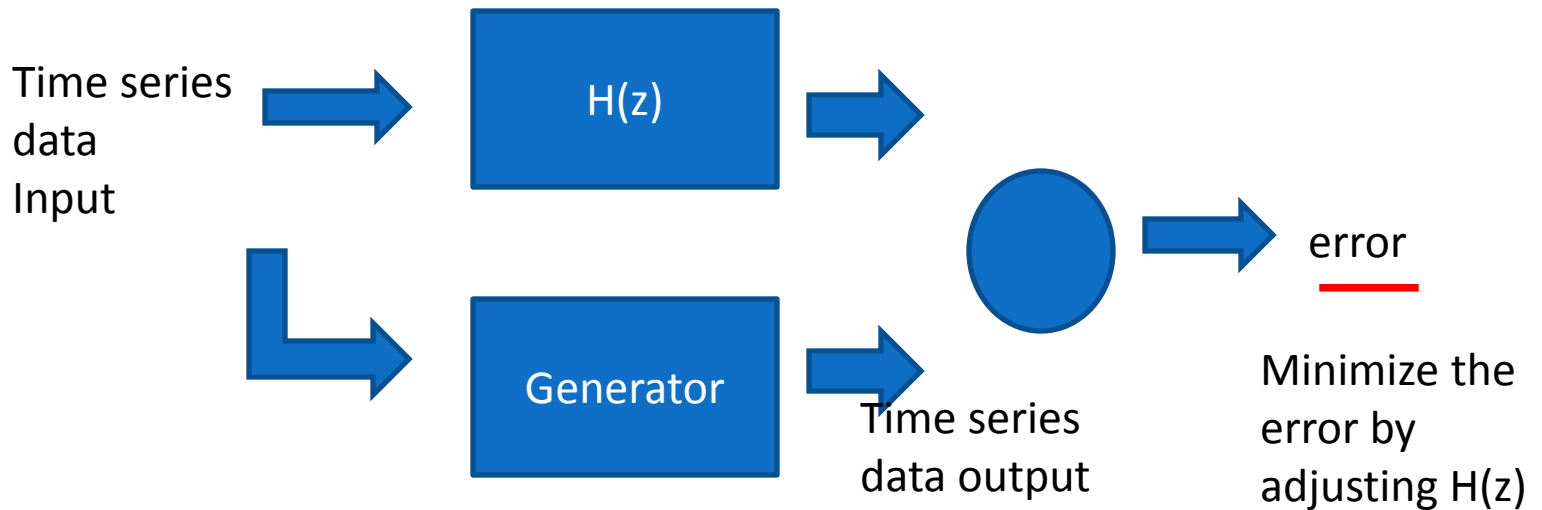
- States and parameters related to **electromagnetic** transient (resistance and inductances of armature winding, field resistance, magnetizing inductance)
  - Sampling rate (**many samples per cycle**)
- 
- J. Melgoza, G. Heydt, A. Keyhani, B. Agrawal, and D. Selin, "Synchronous machine parameter estimation using the hartley series," IEEE Trans. Energy Convers., vol. 16, no. 1, pp. 49–54, mar 2001.
  - E. Kyriakides, G. Heydt, and V. Vittal, "Online parameter estimation of round rotor synchronous generators including magnetic saturation," IEEE Trans. Energy Convers., vol. 20, no. 3, pp. 529–537, sep 2005.
  - J. Melgoza, G. Heydt, A. Keyhani, B. Agrawal, and D. Selin, "An algebraic approach for identifying operating point dependent parameters of synchronous machines using orthogonal series expansions," IEEE Trans. Energy Convers., vol. 16, no. 1, pp. 92–98, mar 2001.
  - E. Kyriakides, G. Heydt, and V. Vittal, "On-line estimation of synchronous generator parameters using a damper current observer and a graphic user interface," IEEE Trans. Energy Convers., vol. 19, no. 3, pp. 499–507, sep 2004.

# PMU data

- 30 Hz or 60 Hz
- Voltage/current magnitude and synchronized phase angles
- Can capture dynamics in phase angles and frequencies
- Make estimation of states and parameters related with electro-mechanical dynamics possible

# Two general methods in state or parameter estimation

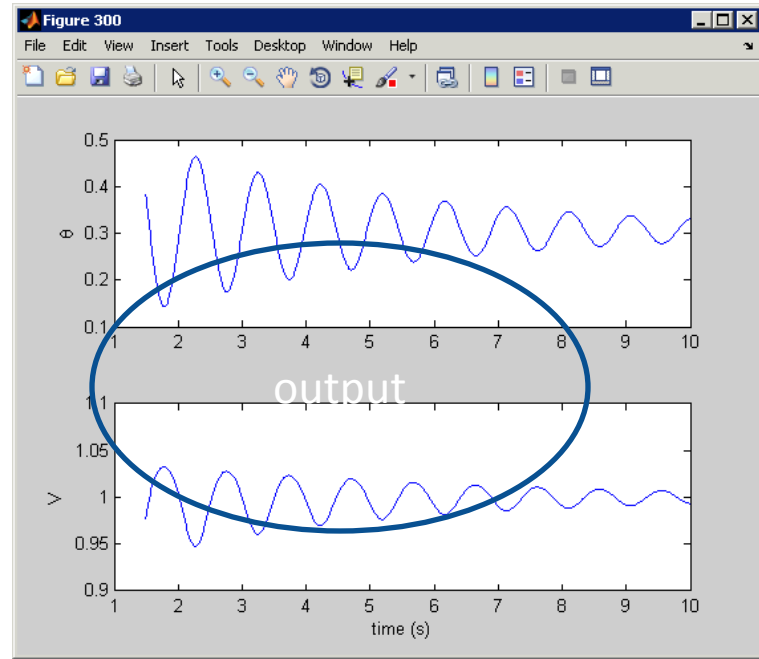
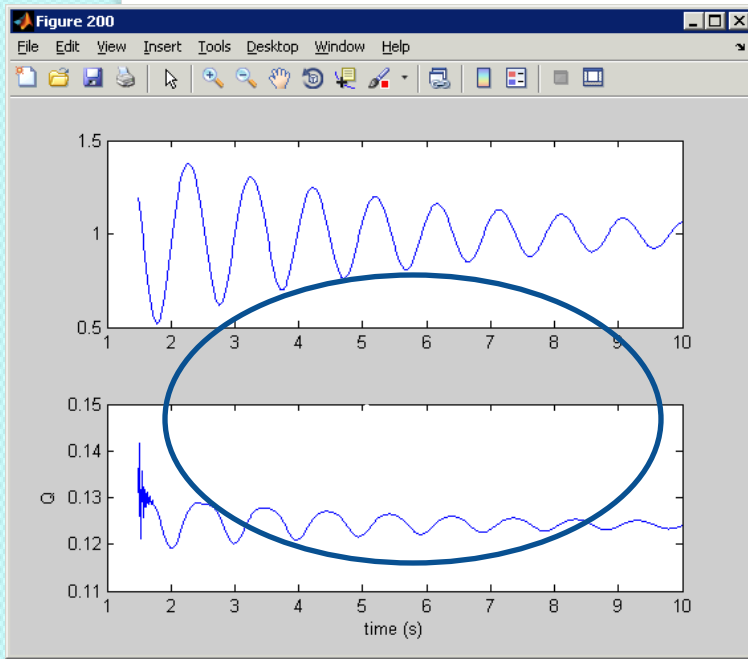
- Given a time window of data (input and output), determine parameters of the transfer function to have least squared error between estimation and measurement. –Matlab System Identification Toolbox

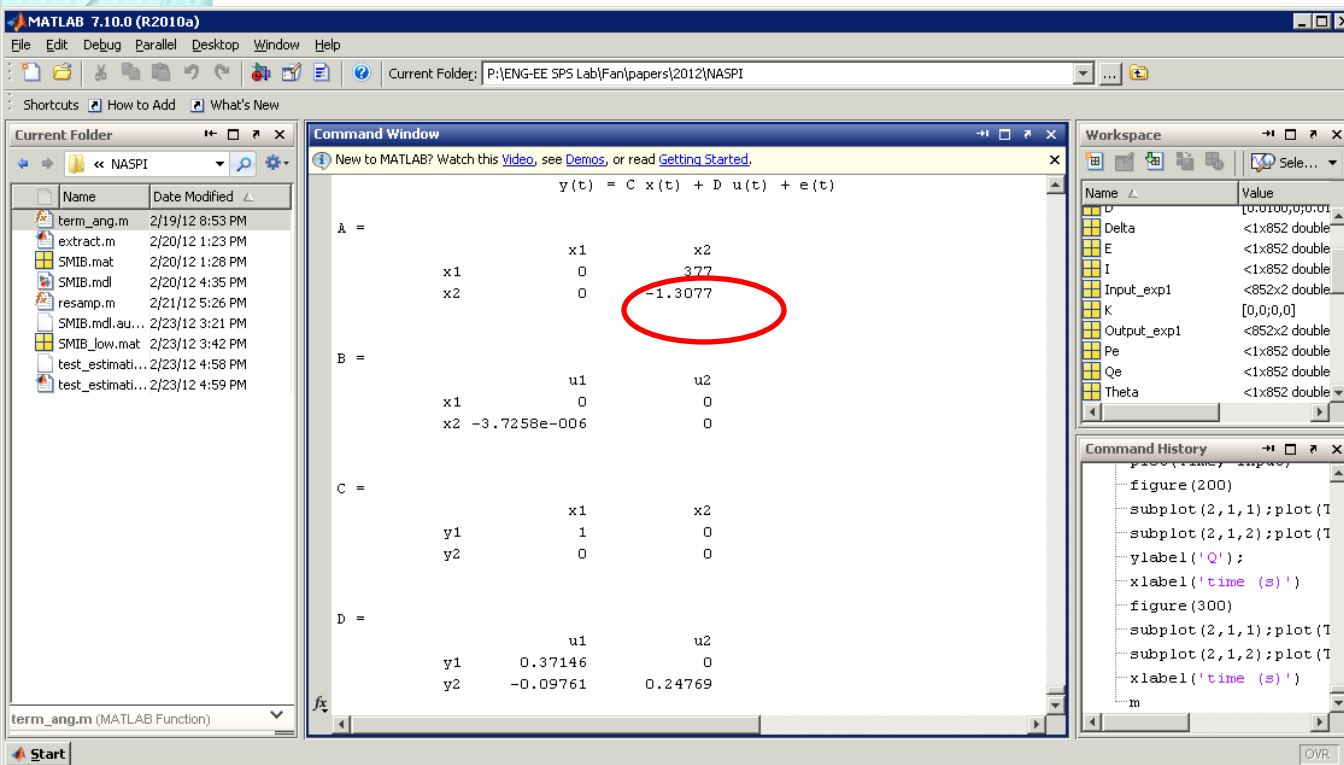


# Structured state-space model estimation

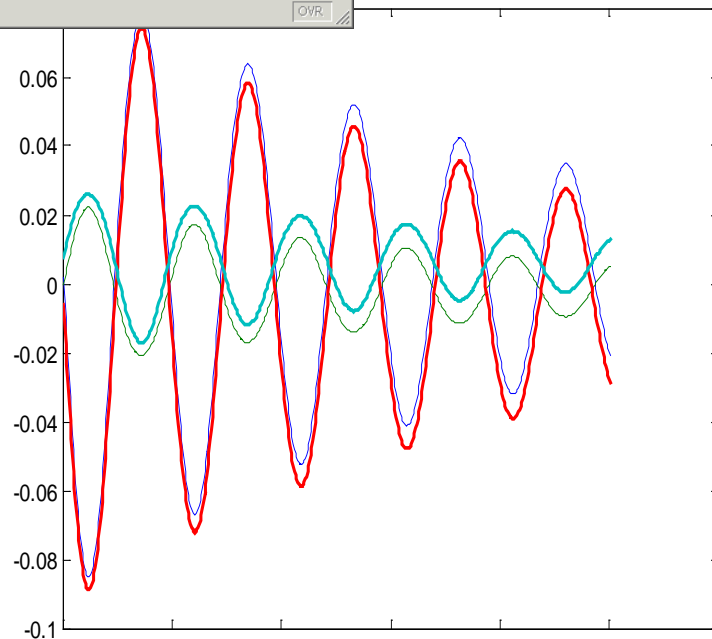
$$\begin{bmatrix} \dot{\Delta\delta} \\ \dot{\Delta\omega} \end{bmatrix} = \begin{bmatrix} 0 & \omega_0 \\ 0 & -\frac{D}{2H} \end{bmatrix} \begin{bmatrix} \Delta\delta \\ \Delta\omega \end{bmatrix} + \begin{bmatrix} 0 & 0 \\ -\frac{1}{2H} & 0 \end{bmatrix} \begin{bmatrix} \Delta P \\ \Delta Q \end{bmatrix}$$

$$\begin{bmatrix} \Delta\theta \\ \Delta V \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \Delta\delta \\ \Delta\omega \end{bmatrix} + \begin{bmatrix} C_1 & C_2 \\ C_3 & C_4 \end{bmatrix} \begin{bmatrix} \Delta P \\ \Delta Q \end{bmatrix}$$



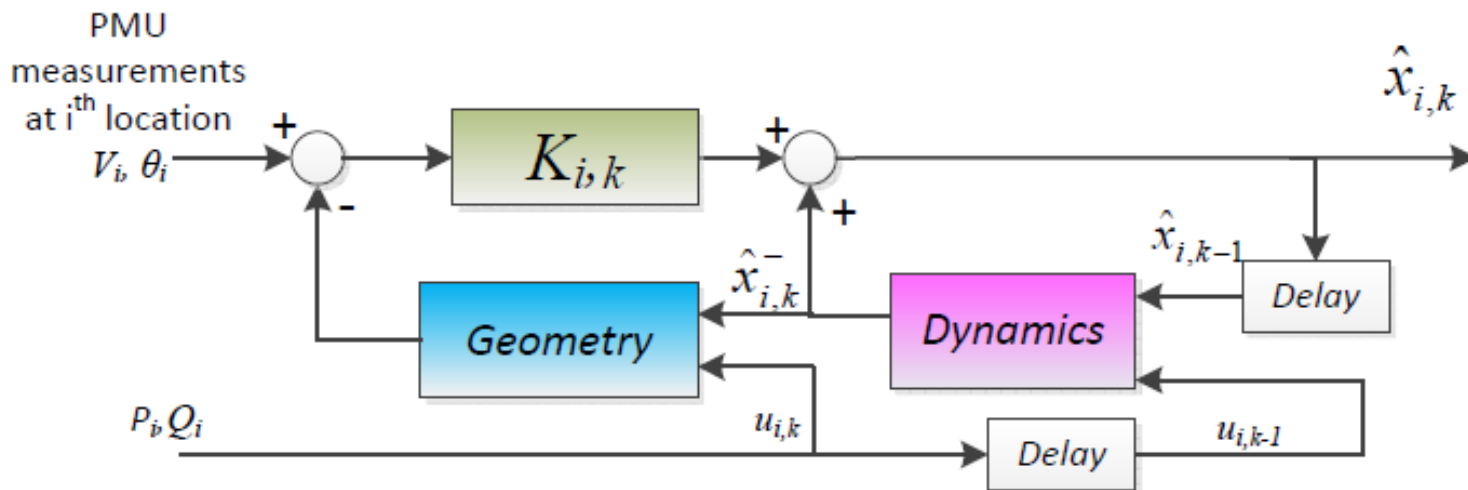


Measurements and simulated results from the estimation model:



# The other general method

- **Kalman filter** - Classical Kalman filter is the optimal minimum mean square estimator when the observations are continuously available



The current step estimation is determined by the previous step estimation and current step measurement only. Estimates are given at “real-time” or every simulation step.

**Previous applications:** machine circuit parameters (Heydt), voltage magnitude and frequency (A. Gigs)

**PMU data:** PNNL

**Feature:** model sensitivity



# How does it work?

$$\hat{x}_{k+1} = A_k \hat{x}_k + B_k u_k + w_k$$

$$\hat{y}_{k+1} = C_{k+1} \hat{x}_{k+1} + D_{k+1} u_{k+1} + v_k$$

Kalman Gain

1. prediction based on last estimate:

$$\hat{x}_{k+1}^- = A_k \hat{x}_k + B_k u_k$$

$$\hat{y}_{k+1} = C_{k+1} \hat{x}_{k+1}^- + D_{k+1} u_{k+1}$$

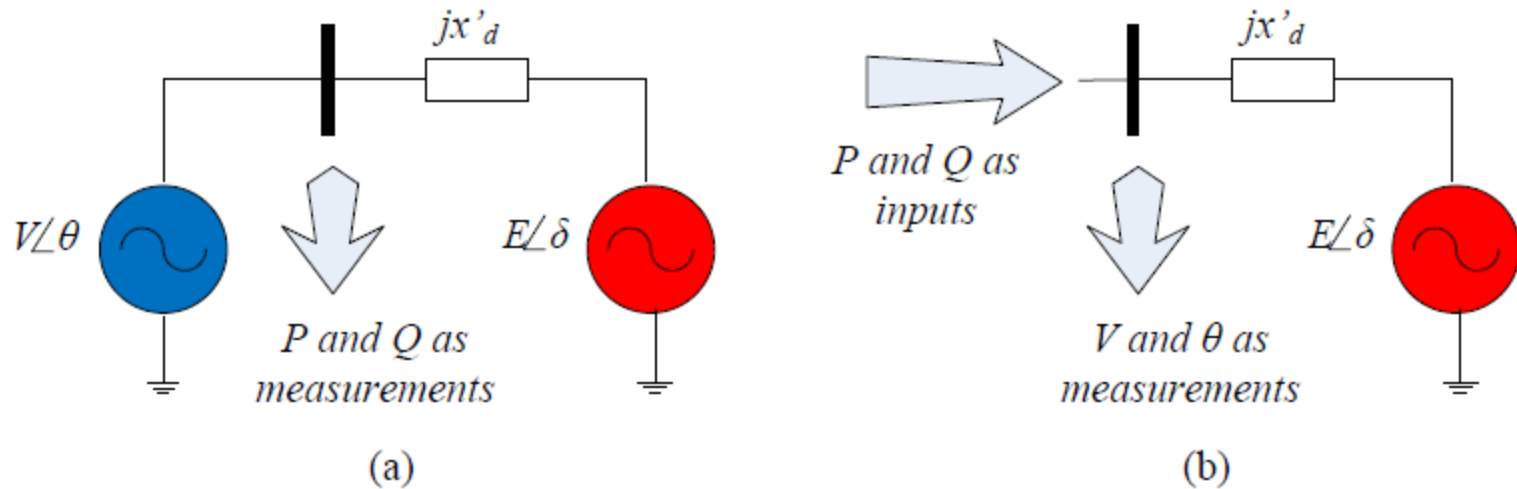
2. calculate correction based on prediction and current measurement:

$$G_k (y_{k+1} - C \hat{x}_{k+1}^- - D u_{k+1})$$

3. update prediction:

$$\hat{x}_{k+1} = \hat{x}_k^- + G_k (y_{k+1} - C \hat{x}_{k+1}^- - D u_{k+1})$$

# Model decoupling



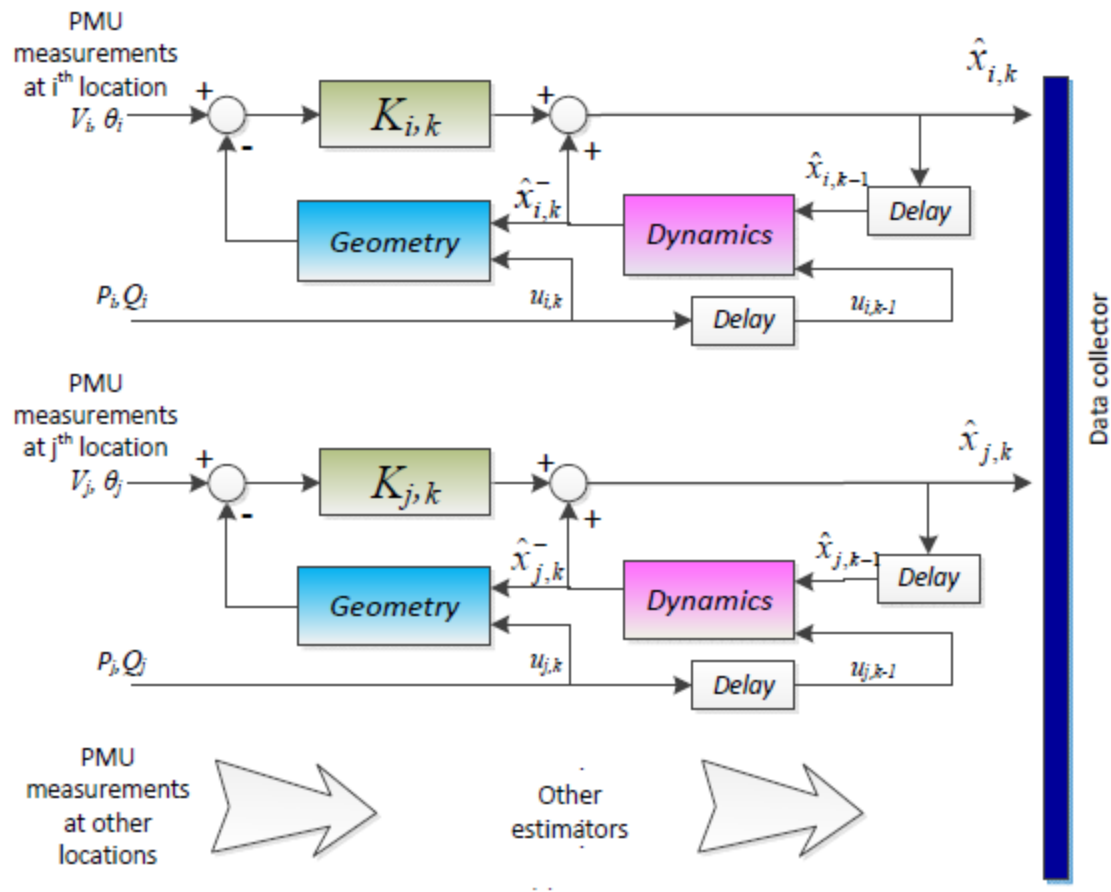
Reduce estimation model  
Estimate a subsystem a time

**Measurement:**  $(V, \theta, P_e, Q_e)$

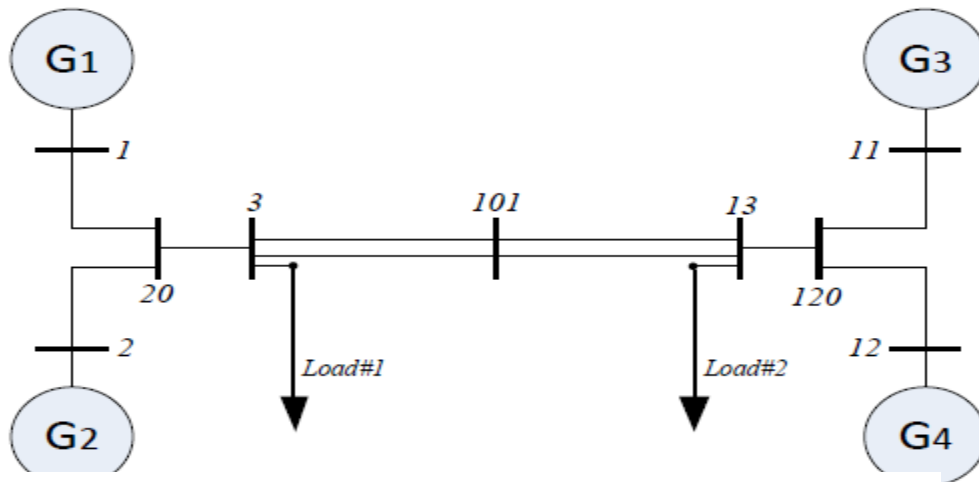
**Estimation 1:** 2 states (angle, speed) 4 parameters (H, D, Pm,  $x_d'$ )

**Estimation 2:** 2 states (angle, speed) 5 parameters (H, D, Pm,  $x_d'$  and E)

# Parallel computing



# Case study: Extended Kalman filter

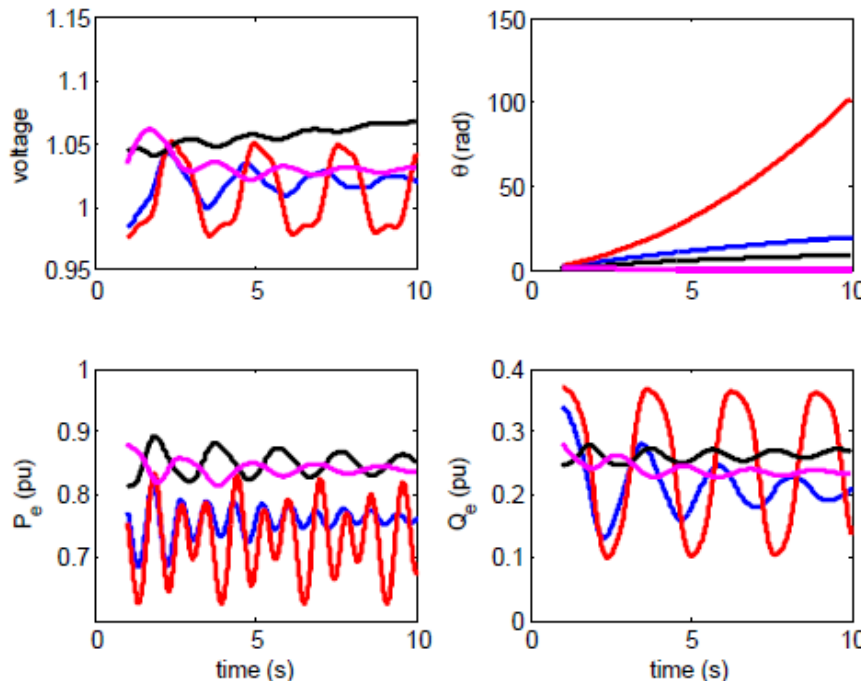


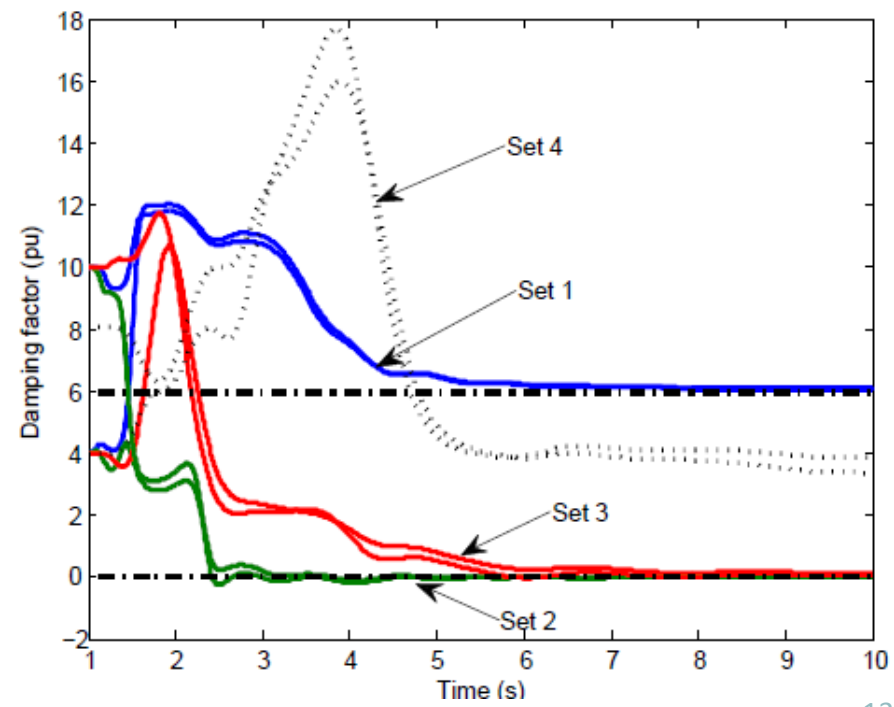
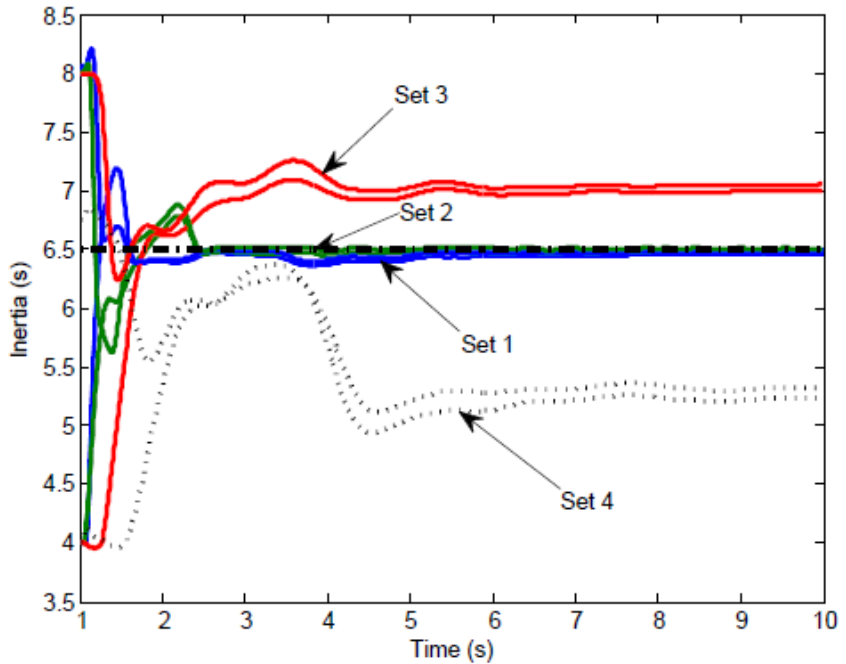
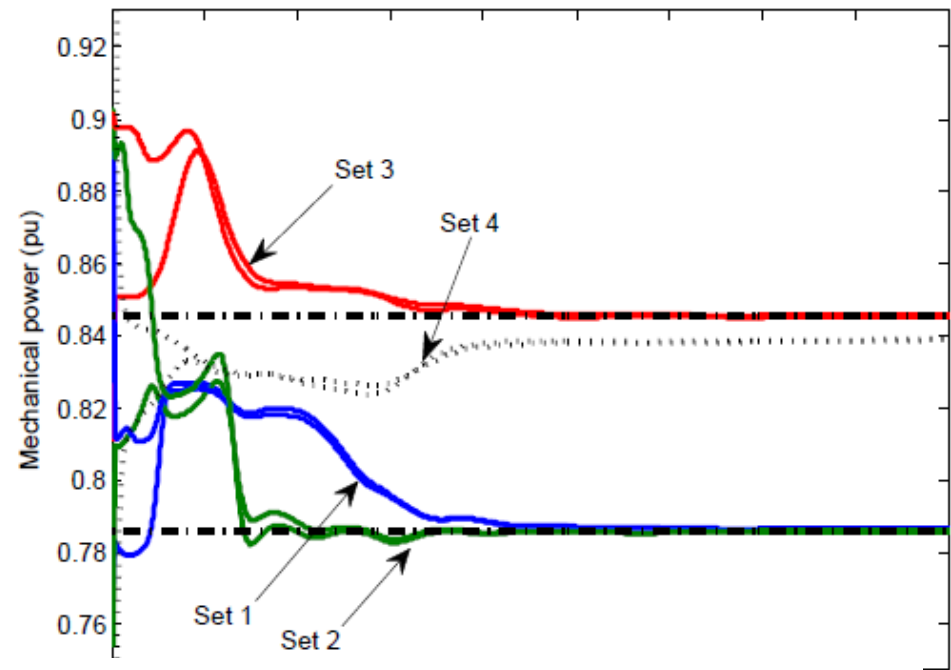
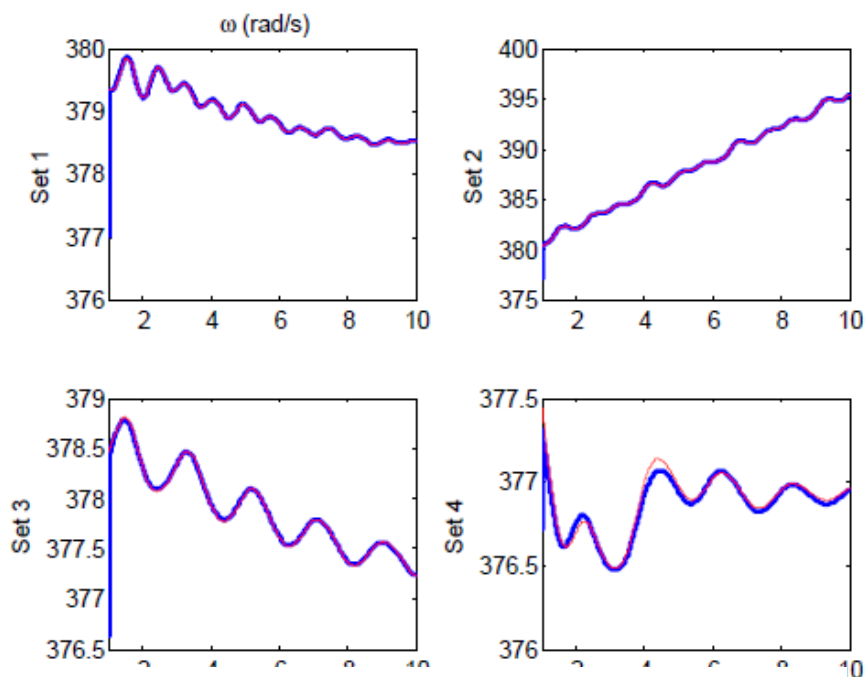
**Red:** classical generator models

**Blue:** In the second set, the damping is reduced to zero in the swing equation.

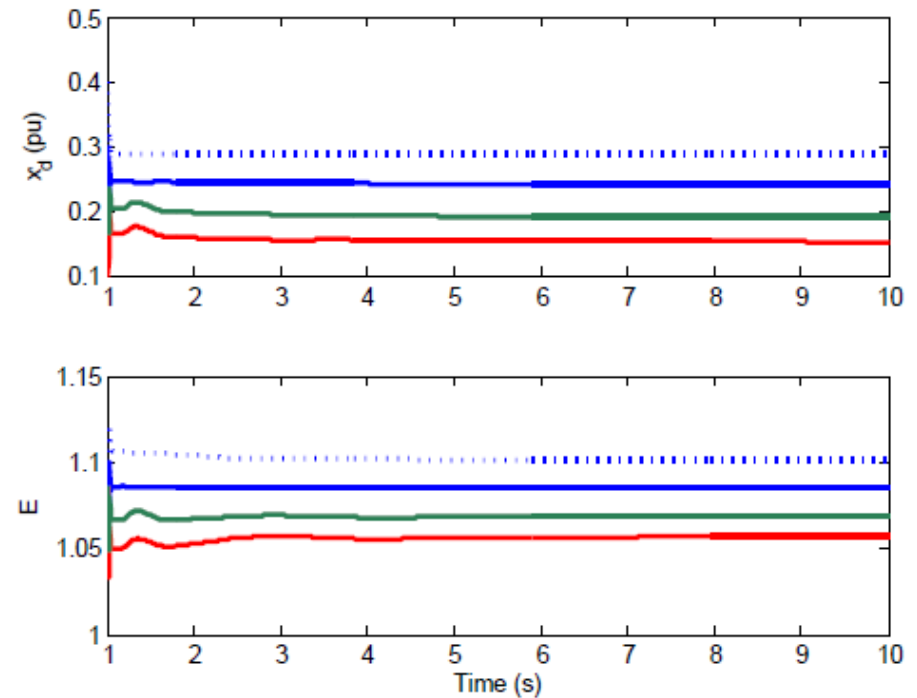
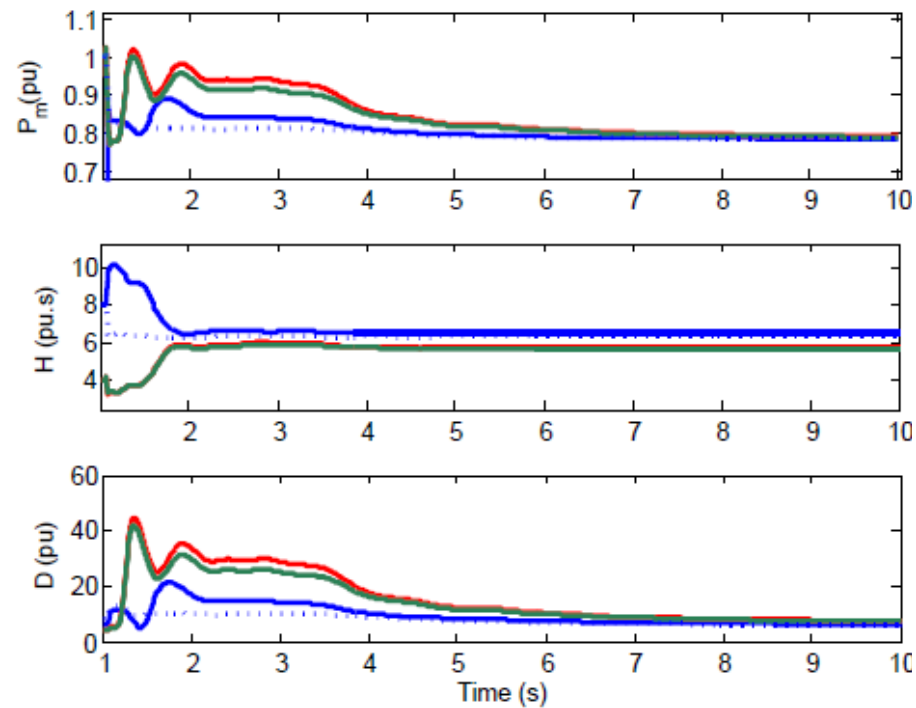
**Black:** In the third set, subtransient generator model is used.  $D=0$

**Magenta:** In the fourth set, subtransient generator model is used.  $D=6$ . AVR enabled





# Estimation 2



Different initial condition  $\rightarrow$  different converged E and  $x'd$   
5 parameter estimation is not feasible

# Questions?

- Thank you!
- Contact [linglingfan@usf.edu](mailto:linglingfan@usf.edu).